Source of Rate Acceleration for Carbocation Cyclization in Biomimetic Supramolecular Cages

Quynh Nhu N. Nguyen,† Kay T. Xia,† Yue Zhang,† Nanhao Chen,† Mariko Morimoto,† Xiaokun Pei, Yang Ha, Jinghua Guo, Wanli Yang, Lee-Ping Wang, Robert G. Bergman,*, Kenneth N. Raymond,*, F. Dean Toste,* and Dean J. Tantillo*

ABSTRACT: The results of quantum chemical and molecular dynamics calculations reveal that polyanionic gallium-based cages accelerate cyclization reactions of pentadienyl alcohols as a result of substrate cage interactions, preferential binding of reactive conformations of substrate/H₂O pairs, and increased substrate basicity. However, the increase in basicity dominates. Experimental structure–activity relationship studies in which the metal vertices and overall charge of the cage are varied confirm the model derived via calculations.

INTRODUCTION

Carbocations are involved as intermediates in catalytic reactions accomplished by both synthetic chemists and biological systems. The latter are most prominently found in the realm of terpene biosynthesis, where terpene synthase enzymes generate carbocations in productive conformations, allowing them to rearrange while protecting them from premature deprotonation or addition by nucleophiles and allowing them to be deprotonated at specific positions (Scheme 1, top, OPP = diphosphate).¹ Synthetic chemists have developed systems that mimic these characteristics.²,³ In both the synthetic and biosynthetic realms, however, the relative importance of each step in the reaction mechanism is still up for debate. Extensive computational work has targeted the issue for terpene synthases,⁴,⁵,⁶ but much less attention has been afforded to synthetic systems.⁷,⁸,⁹

Here, we describe molecular dynamics (MD) and quantum chemical computations on a four-electron electrocyclization of pentadienyl carbocations promoted by the tetrahedral Ga₄L₆ cage studied by Raymond, Bergman, Toste, and co-workers (Scheme 1, bottom).² The cyclization of dienol 1 (multiple geometric isomers have been examined; only one is shown) typically requires strong Lewis or Bronsted acids in bulk solution to promote protonation of oxygen and generate a pentadienyl carbocation intermediate (2), which then undergoes a four-electron electrocyclic ring closure. Under Ga₄L₆-catalyzed conditions, the hydrophobic substrate 1 is first reversibly bound in the naphthalene-walled host cavity, which enables protonation of the alcohol despite the basic aqueous medium outside the host. The substrate ionizes to release water before undergoing four-electron electrocyclization (associated with the highest energy transition state along the reaction coordinate), followed by proton loss to generate the cyclopentadienyl product 3. Due to the similar association

constant of the product (3) and substrate (1), excess maleimide was added to trap the product as the Diels–Alder adduct 4, which no longer is encapsulated by the host.

Our results indicate the essential role of the catalyst cage in promoting carbocation formation primarily via leaving group basicity enhancement. We also conducted a comprehensive experimental study to validate the model derived from calculations and determine the contribution of the metal vertices to supramolecular catalytic activity. We found that when the overall charge of the host was held constant, changing the metal center had little effect on the host’s catalytic performance. Our results provide evidence that supramolecular hosts can tolerate systematic structural modifications without significant loss of catalytic activity.

Computational Methods. Finding a computational approach for modeling such a large system that strikes the right balance between accuracy and efficiency is a challenge. Inspired by the success of Nitschke and co-workers in computing geometries for related cage structures,⁸ we first examined the feasibility of employing various density functionals with relatively small basis sets (see the Supporting Information for details). Ultimately, we found that the B3LYP/3-21G level of theory,⁹ with the LANL2DZ basis set for Ga,⁸ provided reasonable results, suitable for surveying a wide range of structures. Optimizing geometries and computing vibrational frequencies with ostensibly “better” levels of theory proved, in our hands, to be impractical at best and intractable

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at worst. However, single point energies on B3LYP/3-21G-LANL2DZ geometries with various other functionals and larger basis sets showed that the results described below were not very sensitive to the method used (see the Supporting Information); all led to the same qualitative conclusions. In addition, for substrates in the absence of the cage, we performed optimization and frequency calculations with a variety of methods and larger basis sets; results were again very similar to those obtained with B3LYP/3-21G (see the Supporting Information). All calculations were conducted using the conductor-like polarizable continuum model (CPCM) for water (the solvent used experimentally),9 which allowed the cage, which bears a 12\(^{−}\) charge, not to expand significantly beyond its reported crystallographic geometry,\(^{2,10}\) despite the absence of counterions in these calculations. All
reported energies are free energies at 298 K unless stated otherwise. In addition to these static calculations, we carried out MD calculations to address conformational and configurational flexibility. These calculations were set up based on the initial quantum mechanics (QM) optimization results. The organic portions of the cage and the ligand molecules were described by the AMBER general force field, and their charges were calculated by the restrained electrostatic potential (RESP) method based on ESP results obtained with HF/6-31G*. Since there are no parameters for Ga or Si in AMBER, we substituted both by Al for our molecular mechanics (MM) calculations (but set the Si charge to 4+). The assumption that any electronic differences aside from the charge between Ga and Si are insignificant is validated experimentally. All system preparations were done using the tleap program in AMBER. In the MM/MD simulations, a multistep strategy was used to heat and equilibrate the system gradually. First, energy minimization was carried out, followed by a 100 ps heating process (NVT ensemble). Then, another 100 ps MD simulation was carried out to balance the system (NPT ensemble with the help of the Berendsen barostat). Finally, a 50 ns MD simulation (NVT ensemble) was carried out. During the heating and equilibrium processes, an extra force was first added to the cage to prevent its contraction, and the SHAKE algorithm was applied to constrain covalent bond lengths involving hydrogen. The cutoff values for short-range electrostatic and van der Waals interactions were set to 12 Å, and the particle-mesh Ewald method was used for long range summation of electrostatic interactions. All MD calculations were carried out using the OpenMM package.

In addition, to estimate energy barriers for leaving group activation and departure, combined QM/MM calculations were carried out using the Q-Chem and AMBER software packages. The QM region was set as the guest molecule, one H2O* and two H2O molecules that engage in hydrogen-bond interactions with H2O*. All atoms in the QM region were treated with B3LYP/6-31G*, and all the non-QM atoms were described by the force field mentioned above with a 12 Å cutoff for nonbonded interactions. QM/MM free energy calculations made use of umbrella sampling along with the defined reaction coordinate (vide infra) and the weighted histogram analysis method.

## RESULTS AND DISCUSSION

**Effects of Cage Walls on Cyclization.** Raymond, Bergman, and co-workers observed rate accelerations of approximately six orders of magnitude for various isomers of the substrate shown in Scheme 1 in the presence of the cage. Here, we model the substrate with two E double bonds. First, we address the issue of whether or not direct interactions with the Ga4L6 cage lower the barrier for electrocyclization. The transition state structure (TSS) for electrocyclization in the absence of the cage (but in a water continuum) is shown at the top of Figure 1. A barrier of only ~4 kcal/mol was computed for cyclization from a productive, that is, preorganized, conformer of the reactant. Model calculations (Figure 1, middle and bottom) in the presence of a benzene or naphthalene molecule indicate that the aromatic walls of the cage can provide rate acceleration, although the effect is not large. While the walls interact with the substrate, selective binding of the TSS over the pentadienyl cation intermediate is predicted to amount to <2 kcal/mol, indicating that, at best, the observed large rate acceleration must originate primarily from another source.

**Conformational Preorganization.** Another possible contributor to the observed rate acceleration is reactant preorganization; that is, adopting the productive conformation in solution is accompanied by an energy penalty that is "paid" by the catalyst upon binding. Our density functional theory (DFT) calculations suggest, however, that coiled conformers of the substrate, its O-protonated form, and the pentamethylpentadienyl cation (where the two end carbons of the pentadienyl system are near each other) are within ~2 kcal/mol of the lowest energy conformer. For the carbocation, this is the lowest energy conformer. Our MD simulations indicate that pentamethylpentadienyl in explicit water rapidly explores both extended and compact conformations (Figure 2, top). Upon complexation, it still explores these conformations, although transitions between them are not as smooth (Figure 2, middle). The barrier for transitioning between extended and compact forms inside the cage is estimated to be ~3 kT (roughly 2 kcal/mol at room temperature), while outside the cage, the barrier is close to 0 (energy plot shown in the Supporting Information). In general, as water molecules flow into the cage, the conformation of the guest changes from extended to compact. Overall, there appears to be no significant preorganization induced by the catalyst for the alcohol. Pentamethylpentadienol along with an explicit hydroxymion next to the hydroxyl group of the substrate was also modeled with MD (Figure 2, bottom). In this case, the substrate mainly adopts a relatively compact conformation, suggesting that the alcohol/H2O* pair is preferentially accommodated in orientations productive for the reaction.

**Leaving Group Activation—Setting the Stage.** That leaves us with leaving group activation. However, an important issue to address in this regard is the number of water molecules contained within the cage, along with any substrates. Warshel and co-workers previously examined the binding of four water molecules plus one H2O* molecule within the same cage examined here. Based on preliminary DFT calculations, we find that additional water molecules can be encapsulated
without major distortions to the cage geometry (see the Supporting Information). We also addressed this issue with MD simulations of the cage surrounded by water molecules that can enter and leave its interior. Without the substrate present, a range of 0–16 water molecules were observed inside the cage over the length of the MD simulation, while 10–13 water molecules were the most common number (the cage was restrained to prevent shrinking). Recent experimental evidence pointed to 9 ± 1 water molecules in the cage in question.5e With the pentamethylpentadienol substrate present in the cage, 0–4 water molecules were observed in the MD simulation (Figure 3, left, “substrate” bars). When a hydronium ion was included during MD, 2–5 water molecules were present in the cage along with the substrate (the water count does not include the hydronium ion; Figure 3, left, “substrate + hydronium” bars). With the O-protonated pentamethylpentadienol ligand present, 2–6 water molecules were observed inside the cage (Figure 3, left, “cation” bars). A representative snapshot showing the substrate with H_3O^+ and three water molecules in the cage is shown on the right-hand side of Figure 3. The hydronium ion shown is poised to protonate the substrate, while other water molecules inside the cage form a H-bond network.

Figure 2. Distance between alkene carbons that will form the new C–C bond vs time during MD simulations. Top: Pentamethylpentadienol in water. Middle: Pentamethylpentadienol in the cage. Bottom: Pentamethylpentadienol with hydronium ion in the cage.
Leaving Group Activation—Protonation. We begin by discussing DFT (B3LYP/3-21G-LANL2DZ) results on an encapsulated pentamethylpentadienol substrate (Scheme 1), along with various numbers of water molecules and one H$_3$O$^+$ molecule. For these calculations, waters were placed manually near the substrate’s hydroxyl group and allowed to relax into the nearest potential energy surface minimum; a consistent solvent configuration was used for all structures. Calculations with different numbers of water molecules and alternative orientations produced qualitatively similar results (see the Supporting Information for details).

First, we focused on the degree to which the substrate protonation event is affected by the Ga$_4$L$_6$ cage. To do so, we calculated the free energies associated with protonation of the pentamethylpentadienol reactant inside and outside the cage (both in a water continuum), with various numbers of explicit water molecules present. In all cases, the pentamethylpentadienol reactant was predicted to have a larger (by $\geq 15$ kcal/mol) thermodynamic preference for protonation when encapsulated. We also selected configurations from MD simulations using GROMACS clustering with awareness of the symmetry (using RDKit Cookbook) for DFT computations, and for these, encapsulated species are again predicted to be $\sim 15$ kcal/mol more basic (see the Supporting Information for details). Warshel and co-workers also argued that the cage interior provides a “remarkable case of a low “local pH”,” i.e., encapsulated species are readily protonated. While our computed values here may be overestimates of the $pK_a$ modulation—previous experiments on amine, phosphine, and ester guests indicate that a change in $pK_a$ of 4–5 units, corresponding to 5–7 kcal/mol, can be expected upon encapsulation—it is clear that alcohol basicity is markedly enhanced.

What is the origin of the high acidity of the microenvironment within the Ga$_4$L$_6$ cage? The cage used experimentally has walls made of naphthalene rings, and, as shown in Figure 4a, the electrostatic potential within the cage is more negative than that on the cage’s outer surface. As a result, it is possible that substrate–cage CH–π interactions strengthen upon protonation, leading to increased substrate basicity. To test the contribution of the cage walls, all naphthalene rings and attached amide groups were removed (and the remaining catechol rings were capped with hydrogen atoms (Figure 4b); note that this does not change the overall charge of the system), and the substrate protonation energy was recomputed (the geometry of the cage–substrate complex was not allowed to adjust). These changes led to a reduction in predicted protonation energy when no waters are coencapsulated, i.e., protonation is predicted to be less favorable by 17 kcal/mol, consistent with there being interactions between the π-faces of the cage and the substrate.
the cage and the substrate. However, an increase in protonation energy of approximately the same amount is predicted for the complex of the substrate and four bound water molecules, highlighting the fact that some bound waters tend to engage in OH–π interactions that, presumably, decrease the strength of their interactions with the protonated alcohol.

The contributions of specific cage oxygen atoms to basicity modulation were also examined. Keeping the naphthalene walls but deleting all ortho catechol oxygen atoms, all meta catechol oxygen atoms, or all ortho and meta oxygen atoms along with all gallium atoms (and capping the remaining aromatic carbons with hydrogen atoms), all changes which lead to a neutral truncated cage, decreased the basicity of the bound substrate, in the absence of bound waters, by approximately 15−20 kcal/mmol. This result indicates that both the cage charge and π-rich walls contribute roughly equally to the overall effect in the absence of bound water molecules but are antagonistically coupled.24 However, in the presence of bound waters, some water molecules will intrude on specific cage−substrate interactions (vide infra).

We also examined the proton transfer process using QM/MM calculations. A representative snapshot from our MD simulations is shown in Figure 5 (with the cage removed for clarity). Note that this structure showcases the general observation that encapsulated waters cluster on one side of the hydrocarbon group as a hydronium ion hydrogen bonds to the substrate hydroxyl group and to two encapsulated waters. When a QM/MM scan of the proton transfer transition coordinate is carried out, protonated pentamethylpentadienol results (the dip in the energy plot around r = 0.5), which is predicted to be an endothermic process by ~2.5 kcal/mol, associated with a barrier of ~3 kcal/mol. For comparison, we examined the protonation of several amines, reported previously to have pK_a’s shifted by 4−5 units, using the same approach.10 However, little to no barrier was observed computationally in each case, likely because these species are more basic compared to alcohol, precluding meaningful comparisons (see the Supporting Information for details).

**Leaving Group Activation—Actually Leaving.** What of leaving group loss? Continuing along the scan shown in Figure 5, disconnection of the leaving group inside the cage occurs, resulting in the encapsulated pentamethylpentadienyl cation + 4 H_2O. The barrier for this process is predicted here to be ~6.5 kcal/mol, somewhat higher than expected. In the absence of the cage, once the reactant hydroxyl group is protonated, departure of water is expected to occur with little to no barrier. A TSS was not located for this process (modeling such structures is notoriously difficult at best),25 but a constrained calculation with the breaking bond fixed at 1.9 Å led to a predicted barrier of only 2.5 kcal/mol (note also that in the coiled conformer of O-protonated pentamethylpentadienol, the C–O bond is predicted to be approximately 1.7 Å long). This barrier is similar to the barrier of ~4 kcal/mol estimated previously for this type of reaction.26 Nonetheless, the overall barrier from the alcohol to pentamethylpentadienyl cation is predicted to be significantly lower (reduced by ~7 kcal/mol) in the cage than in water (blue versus black traces in Figure 6).

**Changing the Cage Vertices—Predictions and Experimental Validation.** The barrier to form the pentamethylpentadienyl cation is predicted to be 2−3 kcal/mol higher for a cage with Si corners than for a cage with Ga corners (compare Figures 6 and 7), which we ascribe to an electrostatic effect that discourages proton transfer to the substrate since that moves positive charge further from the cage corners (see the Supporting Information for additional details). This predicted barrier difference is consistent with the experimental observation of a 680-fold reduction in the rate associated with changing Ga to Si (for I with two Z alkenes).26 If our simple electrostatic model is reasonable, a rate difference also should be observed for the In/Ge pair of catalyst cages but not the Ga/In and Si/Ge pairs.

**Synthesis of New Cages.** To further confirm the calculated contribution of the charged vertices of the cage to leaving group activation, we sought to compare hosts of
different overall charge and hosts in which the overall charge is maintained but the identity of the metal is changed.

As mentioned above, the metal centers of Ga₄L₆ have previously been replaced to form a catalytically active Si-based host. While it was envisioned that the metal centers could be further diversified to other metals with varied oxidation states, this task presented a major synthetic challenge due to the extreme sensitivity of self-assembly to changes in the structural components. Other catalytically active homogeneous host systems rarely show variability in the metal center. We report here the syntheses of catalytically active Si₄L₆, In₄L₆, and Ge₄L₆ hosts, which were enabled by an optimized and generalizable guest exchange protocol (Figure 8). We then conducted a comprehensive experimental study to confirm the structural similarity of these assemblies and determine the contribution of their coordinatively saturated metal centers to supramolecular catalytic reactivity.

We sought to synthesize the In₄L₆ host to provide an isostructural and homo-anionic comparison to Ga₄L₆. The assembly of In₄L₆ was initially probed by combining 6 equiv of ligand L with 4 equiv of indium trisacetylacetonate in the presence of tetramethylammonium bromide, a strongly binding template. The appearance of six aromatic resonances and a diagnostic upfield-shifted guest resonance in the 1H NMR spectrum confirmed host assembly and encapsulation of the guest (see the Supporting Information). While this was a promising result, a templating guest inhibits host catalysis, and its subsequent removal is hampered by its high association constant. Identifying conditions for a template-free synthesis, however, is often the most challenging step toward accessing these supramolecular catalysts, given the reduced thermodynamic driving force toward host assembly.

Not surprisingly, the assembly of In₄L₆ was not observed in the absence of a templating guest, even upon prolonged heating at 50 °C in methanol. We thus sought an alternative approach, where a weakly binding cationic template such as tetrabutylammonium could be used to first enable self-assembly and subsequently be displaced by potassium counterions to expose the catalytically active host cavity. The guest exchange relies on a large excess of potassium ions to drive the binding equilibrium toward a K⁺-associated host, effectively overcoming the higher association constant of the cationic template. This approach has been previously employed for NMe₄⁺ ⊂ Ga₄L₆, which resulted in relatively poor recovery (36–41% yield) due to the similar solubility profiles of the host and excess KI (the K⁺ source).

Fortunately, the assembly of NMe₄⁺ ⊂ In₄L₆ was observed in the presence of a superstoichiometric amount of tetramethylammonium bromide. Subjecting NMe₄⁺ ⊂ In₄L₆ to guest exchange conditions identical to those used for Ga₄L₆, however, afforded only a trace yield (<5%) of K⁺-associated In₄L₆, prompting an extensive screening to identify conditions for a better protocol. Ultimately, stirring NMe₄⁺ ⊂ In₄L₆ in a saturated solution of KPF₆ in acetone and a small amount of methanol overnight yielded optimal exchange and recovery (Figure 8). Differences in solubility between the host and excess KPF₆ under the reaction conditions enabled nearly quantitative recovery of In₄L₆ by filtration, and after five repeated iterations of the exchange protocol, less than 0.1 equiv of tetramethylammonium remained, as confirmed by 1H NMR spectroscopy (after two rounds of guest exchange, less than 0.2 equiv of NMe₄⁺ remained, yielding a catalytically active host). The stoichiometry and overall charge of In₄L₆ were further verified by electrospray ionization mass spectrometry (ESI-MS), where it was primarily detected in the 3⁻ and 4⁻ charge states with various counterions. Compared to the Ga₄L₆ analogue, In₄L₆ shows an increased sensitivity to oxidation and other decomposition pathways, which was evidenced by rapid attenuation of the signal on ESI-MS.

Next, we turned to the synthesis of Ge₄L₆, which we hoped would provide an isostructural and homo-anionic comparison to Si₄L₆. While the template-free assembly of Ge₄L₆ was not observed, NMe₄⁺ ⊂ Ge₄L₆ could be formed by heating 6 equiv of the ligand and 4 equiv of Ge(IV) methoxide in dimethylformamide in the presence of 5 equiv of NMe₄Br. NMe₄⁺ ⊂ Ge₄L₆ was subjected to the modified guest exchange protocol.

Figure 8. Scheme representing the guest exchange procedure for replacing NMe₄⁺ with K⁺. M = In(III), Ge(IV), or Si(IV). x = 12, 8, or 8, respectively.

Figure 9. Structures obtained by SCXRD of Ga₄L₆, Si₄L₆, and Ge₄L₆. Metal–metal distances are highlighted in green. For Ga₄L₆, the average Ga–Ga distance is 12.663(3) Å and the volume is 239.3(1) Å³. For Si₄L₆, the average Si–Si distance is 12.655(2) Å and the volume is 238.85(6) Å³. For Ge₄L₆, the average Ge–Ge distance is 12.717(3) Å and the volume is 242.39(4) Å³.
conditions which afforded K⁺-associated Ge₄L₆, albeit in lower yields. This decrease in yield was attributed to differences in solubility of In₄L₆ and Ge₄L₆: the lower 8⁻ charge enhances the solubility of Ge₄L₆ in organic solvents such as acetone while slightly decreasing its water solubility. Gratifyingly, addition of a small amount (1 mL) of water to the saturated KPF₆ solution in acetone resulted in the quantitative recovery of Ge₄L₆, which was characterized by ¹H NMR spectroscopy and ESI-MS, detected in the 4⁻ and 5⁻ charge states.

While the template-free synthesis of Si₄L₆ has been shown, it required elevated temperatures, long reaction times (60 h), and rigorous purification. We envisioned that applying the guest exchange protocol would not only serve as a proof-of-concept for the general applicability of the method but could also enable assembly under milder conditions. Indeed, NMe₄⁺⊂Si₄L₆ was quantitatively formed after just 16 h, and guest exchange conditions afforded clean Si₄L₆/K⁺, which could be used without further purification.

Structural data obtained by single crystal X-ray diffraction (SCXRD) confirmed that the cavity size and metal–metal distances were very similar between Ga₄L₆, Si₄L₆, and Ge₄L₆. The crystals of NEt₄⁺⊂Ge₄L₆ were grown by vapor diffusion of benzene into a solution in dimethyl sulfoxide and measured with synchrotron radiation. Like Ga₄L₆ and Si₄L₆, Ge₄L₆ is an ideal tetrahedron, with an average edge length of 12.717(3) Å and a volume of 242.39(4) Å³ (Figure 9). Although we could not obtain SCXRD measurements for In₄L₆, we can expect similarly small deviations in the size and structure of the host as the difference in metal–oxygen bond lengths between these four elements (Ga, Si, Ge, and In) is small (<0.5 Å) compared to the edge length of the tetrahedron. These data demonstrate that the metal–ligand coordination environment is well-preserved between the hosts, confirming their isostructural relationship in the solid state.

In contrast, the total fluorescence yield from the O K-edge soft X-ray absorption spectroscopy (sXAS) data of the four hosts (recorded on BL8.0.1 at the ALS) is shown in Figure 10. Because all the metal ions have filled d manifolds, the pre-edge features of the O K-edge sXAS (between 530 and 535 eV) mainly reflect the transitions from O 1s orbitals to the empty orbitals near the lowest unoccupied molecular orbital (LUMO) with O p characters. The differences in energy splitting and relative intensities imply different electronic structures of the LUMOs, although they all have similar geometric structures. The existence of such differences is supported by the varied assembly conditions that were required when the metal vertices were changed.

### Catalytic Rates

With these four isostructural assemblies consisting of two homo-anionic pairs (12⁻ and 8⁻) in hand, we sought to compare their catalytic activity and observe the effect of changing the metal vertices on the host-catalyzed Nazarov cyclization. Our aim was to determine whether the structural similarity between the hosts would induce similar catalytic behavior or if the electronic differences in metal–oxygen binding would cause divergence. Previous comparison of the Ga₄L₆⁻ and Si₄L₆⁻-catalyzed aza-Cope rearrangement, which proceeds with retention of the cationic charge on the substrate and is driven primarily by constrictive binding within the host, exhibited rates of reaction within error of each other. In₄L₆ and Ge₄L₆ were also shown to catalyze the aza-Cope rearrangement at similar rates to Ga₄L₆ and Si₄L₆, further confirming that structurally similar hosts show no difference in reactivity for a reaction that is not sensitive to changes in host charge (see the Supporting Information). In contrast, the Nazarov cyclization is initiated by protonation of a neutral dienol substrate, resulting in an overall increase in cationic charge within the host microenvironment. Comparison of the Ga₄L₆⁻ and Si₄L₆⁻ catalysts demonstrated a 680-fold difference in rate acceleration, implying that the reaction is indeed sensitive to the host charge. Further investigation of the In₄L₆⁻ and Ge₄L₆⁻-catalyzed reactions should thus enable us to probe the extent to which the identity of the metal affects charge-based supramolecular catalytic reactivity and validate whether the substitution of Al for Ga and Si in the computational model is appropriate.

We investigated the Nazarov cyclization of dienol 1 (with two Z alkenes), which previously demonstrated sensitivity to changes in overall host charge (Scheme 1). Due to the large discrepancy in the rate of the Ga₄L₆⁻ and Si₄L₆⁻-catalyzed reactions, kinetic data were previously obtained at different temperatures and extrapolated for comparison using an Eyring analysis. The In₄L₆⁻-catalyzed reaction could be monitored over the course of a few hours at 45 °C, while the Ge₄L₆⁻-catalyzed reaction required heating to 72 °C to measure the reaction rate on a practicable experimental timescale. This initial observation led us to investigate the four hosts as homo-anionic pairs, where the Ga₄L₆⁻ and In₄L₆⁻-catalyzed reactions were compared at 45 °C, and Si₄L₆⁻ and Ge₄L₆⁻-catalyzed reactions were compared at 72 °C (Table 1).

#### Table 1. Rate Constants (kobs) for the Host-Catalyzed Nazarov Cyclization

<table>
<thead>
<tr>
<th>Catalyst</th>
<th>Catalyst Loading (%)</th>
<th>Temperature</th>
<th>kobs (s⁻¹)</th>
</tr>
</thead>
<tbody>
<tr>
<td>[Ga₄L₆]⁻</td>
<td>7%</td>
<td>45 °C</td>
<td>4.2(3)×10⁻⁴</td>
</tr>
<tr>
<td>[In₄L₆]⁻</td>
<td>10%</td>
<td>45 °C</td>
<td>8.3(1)×10⁻⁴</td>
</tr>
<tr>
<td>[Si₄L₆]⁻</td>
<td>7%</td>
<td>72 °C</td>
<td>2.2(4)×10⁻⁴</td>
</tr>
<tr>
<td>[Ge₄L₆]⁻</td>
<td>6%</td>
<td>72 °C</td>
<td>1.7(1)×10⁻⁴</td>
</tr>
</tbody>
</table>

Figure 10. Oxygen K-edge sXAS data of Ga₄L₆, Si₄L₆, In₄L₆, and Ge₄L₆.
Though the host–dienol Michaelis complex is clearly observable by $^1$H NMR spectroscopy, encapsulation is not quantitative due to the high dissociation constant ($K_d$) of the neutral alcohol substrate. While substrate-dependence studies have not been conducted for the host-catalyzed Nazarov cyclization, it is reasonable to assume that the reaction is not in the saturation regime under these conditions. Thus, the first-order $k_{obs}$ is dependent on the value of the Michaelis constant ($K_m$), which can be approximated by $K_d$. Because small hydrocarbon molecules are encapsulated by the hydrophobic effect, rather than Coulombic attraction, their association is driven primarily by entropic effects.\(^{31}\) Because of this, we expect a negligible difference in $K_d$ of \textit{I} between the two hosts as the host charge plays a minimal role as a driving force for association.

Evidently, the discrepancies in the reaction rates based on the host charge reaffirms the ability of the metal centers to impact catalysis by imparting an overall charge on the host assembly. However, the close agreement in rates between the respective tri- and tetravalent metal centers provides evidence that key electrostatic interactions between the host and the transition state are not significantly perturbed between different homo-cationic metals, consistent with the calculated predictions. These experimental comparisons enable us to pinpoint the specific role of the metal center in catalysis, despite the complexity of structure–activity relationships in multicomponent, self-assembled systems.

The development of an efficient guest exchange protocol enabled high-yielding syntheses of catalytically active $\text{Si}_4\text{L}_{16}$, $\text{In}_4\text{L}_{16}$, and $\text{Ge}_4\text{L}_{16}$ supramolecular hosts. Together with $\text{Ga}_4\text{L}_{16}$, these isostructural catalysts enabled an extensive experimental investigation to isolate the effects of the metal center, an important structural component, on catalytic reactivity. All hosts demonstrated similar catalytic ability for the constrictive-binding-driven aza-Cope rearrangement regardless of the identity or oxidation state of the metal center. While $\text{In}_4\text{L}_{16}$ and $\text{Ge}_4\text{L}_{16}$ hosts demonstrated significant discrepancies in the rate ($k_{obs} = 8.3 \times 10^{-4}$ s\(^{-1}\) at 45°C vs $1.7 \times 10^{-4}$ s\(^{-1}\) at 72°C) for the Nazarov cyclization, reactivity was comparable between hosts with homo-cationic metal centers, in agreement with predictions. These results imply that the structural similarity between the hosts determined their similar catalytic behavior, outweighing the differences in electronic structures implied by the LUMOs with O\(_\pi\) characters indicated by the sXAS data.

**Overall Model.** Thus, we arrive at the following model for rate acceleration. Protonation of the reactant alcohol is greatly enhanced upon complexation, leading to a large net acceleration of water loss. Electrocyclization may be enhanced but only slightly. Warshel and co-workers similarly concluded that selective transition state stabilization was much less significant than reactant protonation for an orthoformate hydrolysis reaction promoted by the Ga\(_4\)L\(_{16}\) cage.\(^\text{Sa,10b}\)

Evidence continues to mount that the reactivity of carbocations generated in the active sites of terpene synthases reflects their energetics in the gas phase.\(^\text{14}\) This was predicted on the basis of results of quantum chemical computations, and multiple experiments withenzymatic systems support this model.\(^\text{32}\) Here, we have shown that a very similar scenario occurs for the Ga\(_4\)L\(_{16}\) cage; the cage facilitates formation of a pentadienyl carbocation, but barrier lowering is not at all necessary for the cyclization reaction step. While type 1 terpene synthase enzymes activate their substrates’ leaving groups (diphosphate groups) primarily by binding to Lewis acidic magnesium ions,\(^\text{14}\) the Ga\(_4\)L\(_{16}\) cage activates its substrates’ leaving groups via facilitation of protonation. Protonation is also used in other (type 2) terpene synthases to generate carbocations from epoxides or alkenes.\(^\text{33}\) In addition to utilizing active-site amino acid sidechains with enhanced acidity (resulting from hydrogen-bonding arrays in which they participate), these terpene synthases provide active site cavities that interact favorably with the carbocations generated upon protonation. Like the Ga\(_4\)L\(_{16}\) cage, these active sites are lined with aromatic amino acid sidechains that can participate in carbocation–\(\pi\) interactions;\(^\text{34a,22,34}\) however, the cage also appears to bind to several water molecules along with the substrate.\(^\text{30c}\) While waters do sometimes bind along with substrates for terpene synthases, they tend to be fewer in number.

**CONCLUSIONS**

Supramolecular catalysis systems remain challenging to model due to the large number of atoms involved and the significant influence of noncovalent and solvent interactions. Our work shows agreement between calculation and experimental data on structure–activity relationships, a promising example of the computational modeling of a complex supramolecular system.

**ASSOCIATED CONTENT**

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/jacs.2c04179.

Details of computational methods and structures; general procedures, synthesis, and characterization of compounds; general procedures for kinetics experiments; representative spectra and kinetics data; ESI-MS data; crystallographic analysis of Ge\(_4\)L\(_{16}\); and \(^1\)H NMR spectra (PDF)

Accession Codes

CCDC 2088585 contains the supplementary crystallographic data for this paper. These data can be obtained free of charge via www.ccdc.cam.ac.uk/data_request/cif, or by emailing data_request@ccdc.cam.ac.uk, or by contacting The Cambridge Crystallographic Data Centre, 12 Union Road, Cambridge CB2 1EZ, UK; fax: +44 1223 336033.

**AUTHOR INFORMATION**

Corresponding Authors

Robert G. Bergman — Department of Chemistry, University of California, Berkeley, California 94720, United States; Chemical Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, United States; orcid.org/0000-0002-3105-8366; Email: rbergman@berkeley.edu

Kenneth N. Raymond — Department of Chemistry, University of California, Berkeley, California 94720, United States; Chemical Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, United States; Email: raymon@soocrates.edu

F. Dean Toste — Department of Chemistry, University of California, Berkeley, California 94720, United States; Chemical Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720, United States; orcid.org/0000-0001-8018-2198; Email: fdtoste@berkeley.edu
Author Contributions

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